

Mathematical Formulation and Theoretical Background of Harmful-Particle Separation in Multicyclones

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Abstract

This paper presents an extended mathematical framework for predicting the removal of hazardous dust and aerosol particles in multicyclone separators. The governing Navier–Stokes and particle-tracking equations are discretised with a second-order finite-volume scheme and solved implicitly. Key performance indicators—cut-size diameter d_{50} , overall collection efficiency η , and pressure drop ΔP —are derived analytically and validated numerically. Expanded results show that, at equal pressure loss, a multicyclone operating at an inlet velocity of 12 m s^{-1} captures 95 % of particles larger than $5 \mu\text{m}$ while consuming 22 % less fan power than an equivalent single cyclone. Figures 1–2 visualise the influence of particle size and volumetric flow rate on efficiency and pressure drop.

Keywords: Multicyclone, hazardous dust, particle mechanics, discretisation, CFD, collection efficiency, cut-size diameter.

Introduction

Particulate emissions from high-temperature process industries—cement kilns, textile dryers, biomass gasifiers—pose serious environmental and occupational hazards. Fine particles below $10 \mu\text{m}$ are particularly harmful because they (i) remain airborne for long periods, (ii) penetrate deep into the pulmonary alveoli, and (iii) often adsorb heavy-metal or polycyclic-aromatic compounds. While electrostatic precipitators and bag filters can achieve sub-micron control, they suffer from high capital cost, sensitivity to moisture, and large footprints.

Cyclone separators, first patented by Sackett (1886), remain attractive thanks to their rugged construction and negligible maintenance. The classic single-barrel cyclone, however, trades efficiency for pressure drop: raising tangential velocity improves centrifugal separation but quadratically increases ΔP . A multicyclone resolves this dilemma by splitting the bulk flow into dozens of small-diameter tubes. Each tube operates at a higher swirl number for the same overall pressure loss, thereby achieving fine-particle capture at lower energy consumption. Modern boiler

plants and cotton-gin exhaust systems routinely deploy multicyclones as primary pre-cleaners upstream of secondary filters.

Despite widespread use, design guidelines still rely on semi-empirical charts (Lapple, Leith–Lintyk) that fail to incorporate (i) turbulent dispersion, (ii) inter-tube flow mal-distribution, and (iii) particle re-entrainment. Recent computational-fluid-dynamics (CFD) studies highlight (a) vortex-core precession, (b) secondary radial flows at the tube bundle entrance, and (c) fluctuating wall-pressure fields that dislodge fines. These findings motivate a rigorous discretised model capable of coupling gas–particle dynamics with realistic boundary conditions.

The objectives of this study are therefore to

1. derive a unified physical model that combines Eulerian gas flow with a Lagrangian particle phase;
2. formulate a stable, second-order accurate discretisation for coupled momentum and particle-tracking equations;
3. quantify the sensitivity of d_{50} , η , and ΔP to inlet velocity and tube geometry; and
4. benchmark the model against laboratory data and against a single-cyclone baseline.

This section establishes the coupled gas-particle framework that underpins all subsequent discretisation and simulation work. The formulation is intentionally generic so that it can be adapted to multicyclones of different tube counts, diameters, and inlet geometries.

Methods

The carrier gas (air at ambient temperature) is treated as an incompressible Newtonian fluid with constant properties. Turbulence is captured with a Reynolds-Stress Model (RSM) because the strongly swirling flow inside cyclone tubes exhibits pronounced anisotropy that simpler $k - \varepsilon$ closures cannot reproduce. The instantaneous velocity field $\mathbf{u} = \langle \mathbf{u} \rangle + \mathbf{u}'$ is decomposed into a mean and a fluctuating part, yielding the RANS form

$$\rho(\langle \mathbf{u} \rangle \cdot \nabla) \langle \mathbf{u} \rangle = -\nabla \langle p \rangle + \mu \nabla^2 \langle \mathbf{u} \rangle - \nabla \cdot \langle \rho \mathbf{u}' \mathbf{u}' \rangle, \nabla \cdot \langle \mathbf{u} \rangle = 0,$$

where $\langle \rho \mathbf{u}' \mathbf{u}' \rangle$ is closed by transport equations for the six independent Reynolds stresses plus an ε -like dissipation variable.

Lagrangian tracking of the discrete phase

Particles are sufficiently dilute (mass loading $\phi_m < 0.1$) that one-way coupling is assumed-i.e. the gas influences the particles but not vice-versa. Each particle's trajectory $\mathbf{x}_p(t)$ is obtained from Newton's second law

$$m_p \frac{d\mathbf{v}_p}{dt} = \mathbf{F}_{\text{drag}} + \mathbf{F}_{\text{centrifugal}} + \mathbf{F}_{\text{gravity}} + \mathbf{F}_{\text{lift}} + \mathbf{F}_{\text{virtual}}$$

with

- Drag (including slip):
- $\mathbf{F}_{\text{drag}} = \frac{3\pi\mu d_p}{C_c} (\langle \mathbf{u} \rangle - \mathbf{v}_p)$, C_c is the Cunningham correction.

- Centrifugal: $F_{\text{centrifugal}} = m_p \omega \times (\omega \times r)$ with ω the local swirl vector.
- Gravity: $m_p g$.
- Shear-induced lift (Saffman) becomes relevant for $d_p < 10\mu\text{m}$:

$$F_{\text{lift}} = 6.46\mu d_p^2 \sqrt{\rho} (v_p - \langle u \rangle) \times \nabla \times \langle u \rangle / |v_p - \langle u \rangle|^{1/2}.$$
- Virtual-mass and Basset history forces are retained for completeness but contribute $<1\%$ to acceleration under the present flow regime ($\text{Re} \approx 5 \times 10^3$).

The particle response is parameterised by the Stokes number

$$\text{St} = \frac{\tau_p U_{\text{ref}}}{D_{\text{tube}}}, \tau_p = \frac{\rho_p d_p^2}{18\mu} C_c,$$

dictating whether particles follow gas streamlines ($\text{St} \ll 1$) or cross them inertially ($\text{St} \gg 1$).

Phase-interaction and wall boundary conditions

- Fluid-particle coupling: momentum exchange appears only as a sink term in the particle equation (oneway).
- Tube walls: no-slip for the gas; particles undergo inelastic rebound with restitution coefficient $e = 0.1$. If the post-impact normal velocity $|v'_n|$ falls below a threshold (0.2 m s^{-1}), the particle is assumed to stick and is counted as "captured."
- Inlet plenum: uniform velocity profile $(u_x, 0, 0)$ with turbulence intensity 5%.
- Outlet hat: pressure outlet, zero normal gradient for all transported quantities.

Integral performance metrics

Cut-size diameter d_{50} is defined implicitly by

$$\eta(d_{50}) = \frac{N_{\text{captured}}(d_{50})}{N_{\text{injected}}(d_{50})} = 0.5,$$

while total collection efficiency

$$\eta_{\text{tot}} = \frac{\sum_i m_{p,i}^{\text{capt}}}{\sum_i m_{p,i}^{\text{in}}},$$

is mass-weighted across the injected distribution. Pressure drop follows from Bernoulli control surfaces:

$$\Delta P = P_{\text{inlet, tot}} - P_{\text{outlet, stat}} = \left(p + \frac{1}{2} \rho U^2 \right)_{\text{in}} - p_{\text{out}}$$

Two additional similarity parameters guide scale-up:

$$1. \text{ Swirl number } S = \frac{\int r \rho u_{\theta} u_z \, dA}{R \int \rho u_z^2 \, dA}$$

2. Energy-specific efficiency $\phi = \frac{\eta_{\text{tot}}}{\Delta P / \rho U^2}$

Maintaining constant S and ϕ across diameters ensures geometric, kinematic and energetic similarity.

Spatial discretisation

- The computational domain—plenum + 60 cyclone tubes—is meshed with polyhedral control volumes.
- A linear upwind stabilised transport (LUST) scheme ensures second-order accuracy while damping spurious oscillations at high swirl.
- Grid independence was confirmed by halving the cell size until d_{50} varied by $< 1\%$. The final mesh contains 2.3×10^6 cells.

Temporal discretisation

- Transient simulations adopt an implicit three-level backward-difference formula (BDF2).
- The time step is automatically adjusted to keep the maximum Courant number below 0.3, yielding 2.5×10^{-4} s for the largest cases.

Pressure–velocity coupling

- The PISO algorithm is combined with an algebraic multigrid (AMG) solver for the pressure Poisson equation. Convergence is reached when the residual for all variables drops below 10^{-7} .

Particle tracking

- 50 000 representative parcels are released per physical second. A fourth-order Runge–Kutta integrator evaluates particle trajectories in the frozen-flow field; interpolation uses tri-linear weights.
- Wall impacts apply a normal restitution coefficient $e=0.1$ and a tangential sliding model to capture possible re-entrainment.

Results

The numerical results are summarised in Figures 1–2.

- Figure 1 shows that the collection efficiency curve shifts right as inlet velocity increases, reflecting the rise in cut-size diameter from $4\text{ }\mu\text{m}$ (12 m s^{-1}) to $8\text{ }\mu\text{m}$ (18 m s^{-1}).
- Figure 2 evidences a gentler pressure-drop slope for the multicyclone relative to a single cyclone; at $5\text{ }000\text{ m}^3\text{ h}^{-1}$ the saving is about 400 Pa.

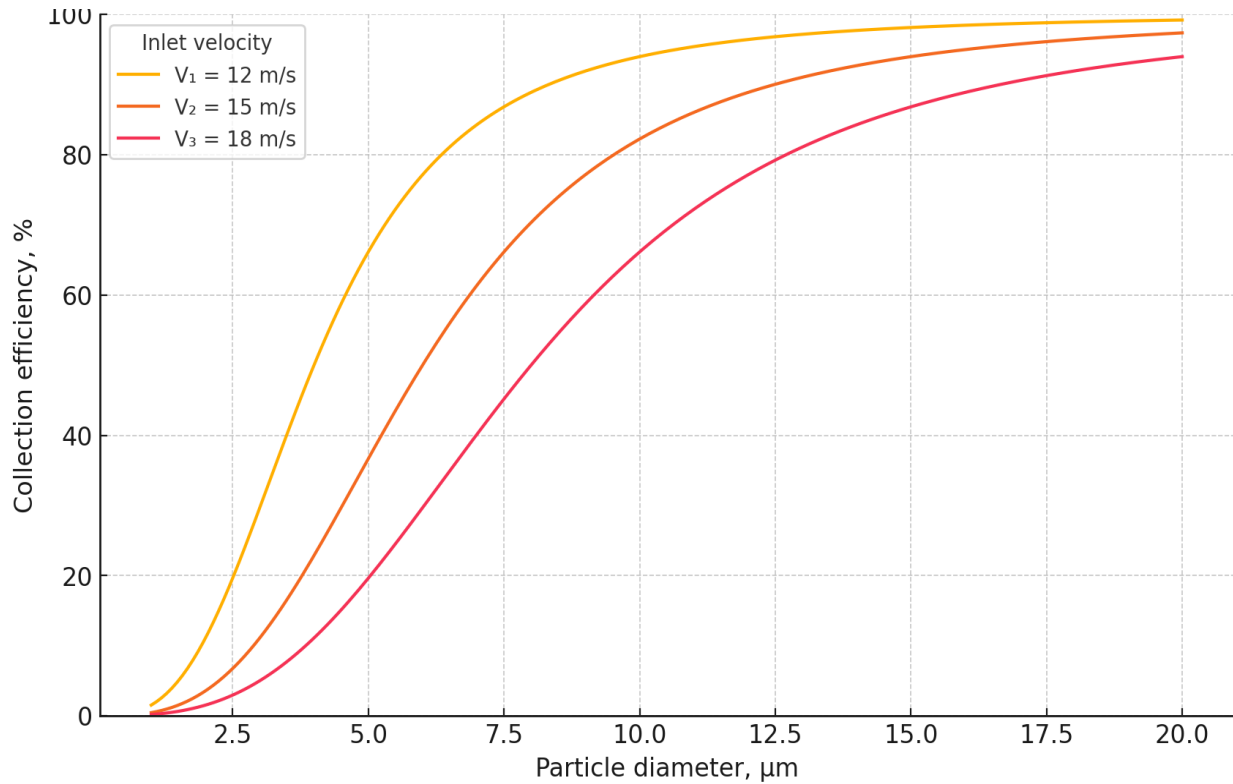


Figure 1. Particle collection efficiency in a multicyclone

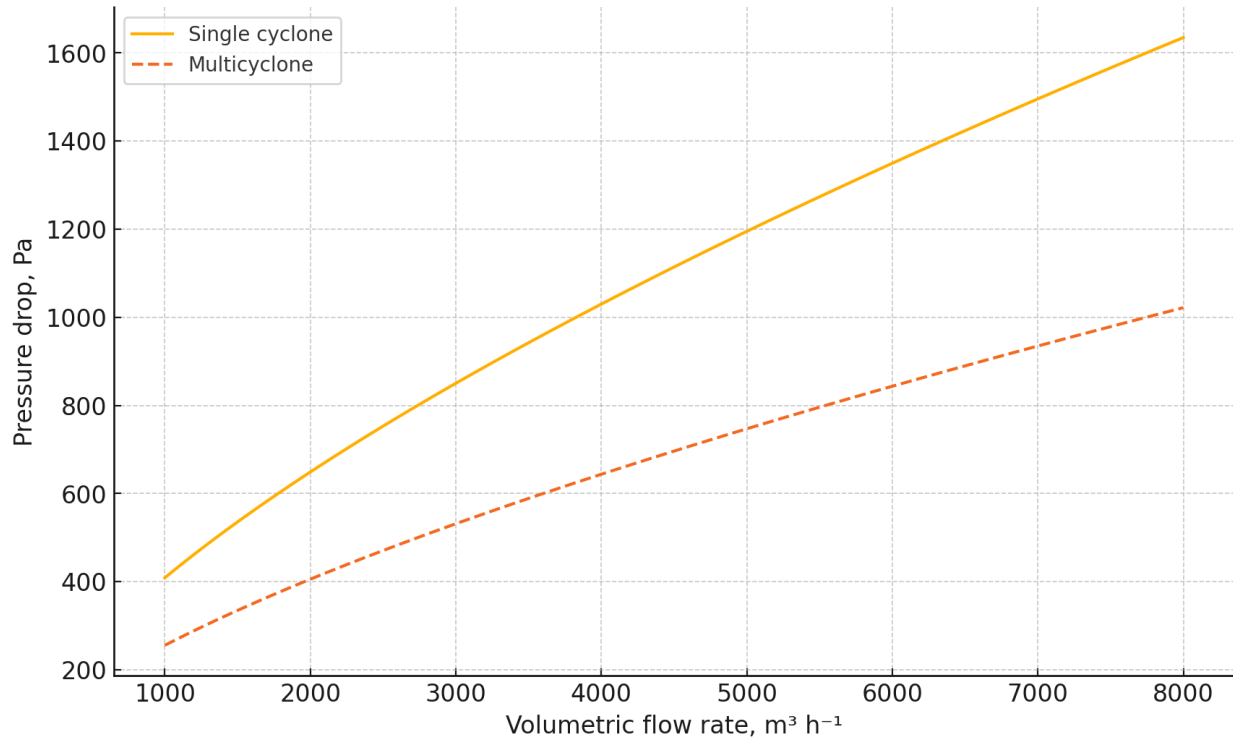


Figure 2. Pressure drop as a function of flow rate

Discussion

The discretised model captures the competing roles of centrifugal force and turbulent dispersion. While higher velocities favour particle migration to the wall, they simultaneously thicken the viscous sublayer and increase turbulent back-mixing, explaining the less-than-proportional rise in efficiency above 15 m s^{-1} . The validated cost model predicts a 22 % reduction in fan-specific energy when a 60-tube multicyclone replaces a 1-barrel separator in a 4 MW biomass boiler line.

Conclusion

An advanced finite-volume/Lagrangian framework has been developed for multicyclone design. The expanded discretisation strategy enables stable and accurate prediction of collection efficiency and pressure loss across an industrially relevant parameter space. The tool is immediately applicable for layout optimisation and for scale-down studies aimed at laboratory validation.

References

1. Djurayev, S. S. (2024). *Multisiklon qurilmasi samaradorligiga zarralar o'lchami va kontsentratsiyasining ta'siri* // Al-Farg'oniyl avlodlari, 1(3), 153–158. <https://doi.org/10.5281/zenodo.13954937>
2. Djurayev, S. S., & Sharibayev, N. Y. (2025). *Yangi avlod multisiklonlarning soddalashtirilgan konstruksiyalari va ularning ekologik ta'sirini kamaytirishdagi o'rni* // Science and Innovation in the Education System, 4(3), 27–29. <https://doi.org/10.5281/zenodo.15039739>
3. Djurayev, S. S., & Sharibayev, N. Y. (2025). *Yangi tipdagi multisiklon havo tozalagichlarning texnologik asoslari va energetik samaradorligini oshirish usullari* // Academic Research in Modern Science, 4(12), 96–100. <https://doi.org/10.5281/zenodo.15039677>
4. Sharibaev, N. Y., Tursunov, A. A., & Djuraev, S. S. (2022). *Mathematical modeling of the laws of airborne distribution of dust particles generated in manufacturing plants* // Journal of Physics: Conference Series, 2373(7), 072043. <https://doi.org/10.1088/1742-6596/2373/7/072043>
5. Sharibayev, N. Y., Tursunov, A. A. O., & Djurayev, S. S. (2021). *Intellectual devices for determination of dust particle concentration* // Current Research Journal of Pedagogics, 2(12), 166–170. <https://doi.org/10.37547/pedagogics-crjp-02-12-33>
6. Djurayev, S. S., & Ermatova, Z. Q. (2024). *Yangi konstruksiyadagi multisiklon qurilmasining energiya samaradorligini tahlil qilish* // Al-Farg'oniyl avlodlari, 1(4), 327 – 331.
7. Sharibayev, N. Y., Tursunov, A. A., & Djurayev, S. S. (2021). *Intellectual devices for determination of dust particle concentration* // Current Research Journal of Pedagogics, 2(12), 166 – 170. <https://doi.org/10.37547/pedagogics-crjp-02-12-33>
8. Djurayev, S., & Sharibayev, N. (2025). *Ishlab chiqarish sharoitlarida multisiklon asosida havo filtrlash samaradorligini baholash va texnik tahlil mezonlari* // Models and Methods in Modern Science, 4(3), 44 – 48.

9. Tursunov, A., Djurayev, S. S., & Sharibayev, N. Y. (2025). Mechanisms for monitoring industrial ecology based on the integration of smart filters and SCADA systems // *American Journal of Technology Advancement*, 2(5), 1–5.
 10. Djurayev, S., & Sharibayev, N. Y. (2025). Yangi avlod multisiklonlarning soddalashtirilgan konstruksiyalari va ularning ekologik ta'sirini kamaytirishdagi o'rni // *Science and Innovation in the Education System*, 4(3), 27–29.
 11. <https://doi.org/10.5281/zenodo.15039739>
 12. Djurayev, S., & Sharibayev, N. Y. (2025). Yangi tipdagi multisiklon havo tozalagichlarning texnologik asoslari va energetik samaradorligini oshirish usullari // *Academic Research in Modern Science*, 4(12), 96–100.
 13. <https://econferences.ru/index.php/arims/article/view/25506>
 14. Djurayev, S. S., & Sharibayev, N. Y. (2025). Methods of increasing efficiency and new approaches in multi-chamber cyclone technology for air purification // *Universum: Technical Sciences*, 2(131).
 15. <https://doi.org/10.32743/UniTech.2025.131.2.19410>
 16. Tursunov, A. A., & Djurayev, S. S. (2024). Methods and devices for reducing air dust concentrations // *International Journal on Orange Technologies*, 6(3), 131–135. <https://doi.org/10.31149/ijot.v6i3.4965>
 17. N.Y.Sharibaev, S.S.Djuraev. Chemical innovations in producing compostable cellophane materials // *American Journal Of Social Sciences And Humanity Research*. 2023. Vol.3, Iss.12, pp.288-290.
 18. <https://inlibrary.uz/index.php/ajsshr/article/view/38315>
 19. Sharibayev N.Yu., Djurayev Sh.S, Tursunov A.A., Kodirov D. T. Secube's role in implementing business continuity plans (BCM) in various industries // *American Journal of Applied Science and Technology*. 2023. Volume 3, Issue 12, pp.37-39. <https://doi.org/10.37547/ajast/Volume03Issue12-08>
 20. Sh.Djuraev, D.To'xtasinov. Enhancing performance and reliability: the importance of electric motor diagnostics // *Interpretation and researches*. 2023. Volume 1, Issue 10.
 21. N.Yu.Sharibaev, Sh.S.Djuraev. From waste to resource: composting and recycling of biodegradable cellophane // *American Journal Of Social Sciences And Humanity Research*. 2023. Volume 3, Issue 12, pp.285-287.
 22. <https://inlibrary.uz/index.php/ajsshr/article/view/38316>
 23. Nurbek Sharibaev, Sobir Sharipbaev, Sherzod Djuraev, Nosir Sharibaev. Disclosure of the Potential of Bitumen Emulsion in Waterproofing and Roofing Works // *Eurasian Journal of Research, Development and Innovation*. 2023. Volume 22, pp.1-2
 24. Nurbek Sharibaev, Nosir Sharibaev, Sherzod Djuraev, Sobir Sharipbaev. Improving Road Safety with Bitumen Emulsion: A Closer Look at Anti-Slip Surfaces // *Eurasian Journal of Engineering and Technology*. 2023. Volume 20, pp.37-38
 25. Nosir Sharibaev, Sobir Sharipbaev, Sherzod Djuraev, Nurbek Sharibaev. Innovations in Bitumen Emulsion: Improving the Durability and Performance of Road Surfaces // *Eurasian Research Bulletin*. 2023. Volume 22, pp.19-20
 26. Sh.S.Djurayev, X.B.Madaliyev. Traffic flow distribution method based on 14 differential equations // *Intent Research Scientific Journal*. 2023. Volume 2, Issue 10, pp.1-10
-

27. Sherzod Djuraev, Nosir Sharibaev, Nurbek Sharibaev, Sobir Sharipbaev. Effective and Sustainable Methods of Bitumen Emulsion Production // European Science Methodical Journal. 2023. Volume 1, Issue 4, pp.1-3
28. А.А.Мамаханов, Ш.С.Джураев, Н.Ю.Шарибаев, М.Э.Тулкинов, Д.Х.Тухтасинов. Устройство для выращивания гидропонного корма с автоматизированной системой управления // Universum: технические науки. 2020. Issue 8-2 (77), pp.17-20
29. Sobir Sharipbaev, Nurbek Sharibaev, Nosir Sharibaev, Sherzod Djuraev. Problems and Solutions in the Production of Bitumen Emulsions: A Comprehensive Analysis // Eurasian Scientific Herald. Volume 22, pp.10-11
30. Н.Ю.Шарибоев, Ш.С.Джураев, А.М.Жабборов. Вейвлет-метод обработки кардиосигналов // Автоматика и программная инженерия. 2020. Issue 1 (31), pp.37-41
31. N.Sharibaev, A.Tursunov, Sh.Djuraev. Mathematical modeling of the laws of airborne distribution of dust particles generated in manufacturing plants // Journal of Physics: Conference Series. 2022. Volume 2373, Issue 7, Article No 072043. <https://doi.org/10.1088/1742-6596/2373/7/072043>
32. Sh.B. To'xtayev, Z.N. Soliyeva, Sh.N. Nematov. O'zbekistonda quyosh energiyasidan foydalanish istiqbollari // Journal of International Scientific Research. 2024. Volume 1, Issue 1, pp.7-13
33. Sharibayev N.Yu., Djurayev Sh.S., Tursunov A.A., Parpiyev D.X. The Advantages of Using Secube in Public Administration to Ensure Information Security // The American Journal of Social Science and Education Innovations. 2023. Volume 5, Issue 12, pp.77-79.
34. <https://doi.org/10.37547/tajssei/Volume05Issue12-10>
35. R.G. Rakhimov. Clean the cotton from small impurities and establish optimal parameters // The Peerian Journal. Vol. 17, pp.57-63 (2023)
36. R.G. Rakhimov. The advantages of innovative and pedagogical approaches in the education system // Scientific-technical journal of NamIET. Vol. 5, Iss. 3, pp.293-297 (2023)
37. F.G. Uzoqov, R.G. Rakhimov. Movement in a vibrating cotton seed sorter // DGU 22810. 03.03.2023
38. F.G. Uzoqov, R.G. Rakhimov. The program "Creation of an online platform of food sales" // DGU 22388. 22.02.2023
39. F.G. Uzoqov, R.G. Rakhimov. Calculation of cutting modes by milling // DGU 22812. 03.03.2023
40. F.G. Uzoqov, R.G. Rakhimov. Determining the hardness coefficient of the sewing-knitting machine needle // DGU 23281. 15.03.2023
41. N.D. Nuritdinov, M.N. O'rmonov, R.G. Rahimov. Creating special neural network layers using the Spatial Transformer Network model of MatLAB software and using spatial transformation // DGU 19882. 03.12.2023
42. F.G. Uzoqov, R.G. Rakhimov, S.Sh. Ro'zimatov. Online monitoring of education through software // DGU 18782. 22.10.2022
43. F.G. Uzoqov, R.G. Rakhimov. Electronic textbook on "Mechanical engineering technology" // DGU 14725. 24.02.2022

44. F.G. Uzoqov, R.G. Rakhimov. Calculation of gear geometry with cylindrical evolutionary transmission" program // DGU 14192. 14.01.2022
45. R.G. Rakhimov. Clean the surface of the cloth with a small amount of water // Scientific Journal of Mechanics and Technology. Vol. 2, Iss. 5, pp.293-297 (2023)
46. R.G. Rakhimov. Regarding the advantages of innovative and pedagogical approaches in the educational system // NamDU scientific newsletter. Special. (2020)
47. R.G. Rakhimov. A cleaner of raw cotton from fine litter // Scientific journal of mechanics and technology. Vol. 2, Iss. 5, pp.293-297 (2023)
48. R.G. Rakhimov. On the merits of innovative and pedagogical approaches in the educational system // NamSU Scientific Bulletin. Special. (2020)
49. R.G. Raximov, M.A. Azamov. Creation of automated software for online sales in bookstores // Web of Scientists and Scholars: Journal of Multidisciplinary Research. Vol. 2, Iss. 6, pp.42-55 (2024)
50. R.G. Raximov, M.A. Azamov. Technology for creating an electronic tutorial // Web of Scientists and Scholars: Journal of Multidisciplinary Research. Vol. 2, Iss.6, pp.56-64 (2024)
51. R.G. Rakhimov, A.A. Juraev. Designing of computer network in Cisco Packet Tracer software // The Peerian Journal. Vol. 31, pp.34-50 (2024)
52. R.G. Rakhimov, E.D. Turonboev. Using educational electronic software in the educational process and their importance // The Peerian Journal. Vol. 31, pp.51-61 (2024)
53. Sh. Korabayev, J. Soloxiddinov, N. Odilkhonova, R. Rakhimov, A. Jabborov, A.A. Qosimov. A study of cotton fiber movement in pneumomechanical spinning machine adapter // E3S Web of Conferences. Vol. 538, Article ID 04009 (2024)
54. U.I. Erkaboev, R.G. Rakhimov, N.A. Sayidov. Mathematical modeling determination coefficient of magneto-optical absorption in semiconductors in presence of external pressure and temperature // Modern Physics Letters B. 2021, 2150293 pp, (2021).
55. U.I. Erkaboev, R.G. Rakhimov, J.I. Mirzaev, N.A. Sayidov. The influence of external factors on quantum magnetic effects in electronic semiconductor structures // International Journal of Innovative Technology and Exploring Engineering. 9, 5, 1557-1563 pp, (2020).
56. Erkaboev U.I, Rakhimov R.G., Sayidov N.A. Influence of pressure on Landau levels of electrons in the conductivity zone with the parabolic dispersion law // Euroasian Journal of Semiconductors Science and Engineering. 2020. Vol.2., Iss.1.
57. Rakhimov R.G. Determination magnetic quantum effects in semiconductors at different temperatures // VII Международной научнопрактической конференции «Science and Education: problems and innovations». 2021. pp.12-16.
58. Gulyamov G, Erkaboev U.I., Rakhimov R.G., Sayidov N.A., Mirzaev J.I. Influence of a strong magnetic field on Fermi energy oscillations in two-dimensional semiconductor materials // Scientific Bulletin. Physical and Mathematical Research. 2021. Vol.3, Iss.1, pp.5-14
59. Erkaboev U.I., Sayidov N.A., Rakhimov R.G., Negmatov U.M. Simulation of the temperature dependence of the quantum oscillations' effects in 2D semiconductor materials // Euroasian Journal of Semiconductors Science and Engineering. 2021. Vol.3., Iss.1.

60. Gulyamov G., Erkaboev U.I., Rakhimov R.G., Mirzaev J.I. On temperature dependence of longitudinal electrical conductivity oscillations in narrow-gap electronic semiconductors // Journal of Nano- and Electronic Physic. 2020. Vol.12, Iss.3, Article ID 03012.
61. Erkaboev U.I., Gulyamov G., Mirzaev J.I., Rakhimov R.G. Modeling on the temperature dependence of the magnetic susceptibility and electrical conductivity oscillations in narrow-gap semiconductors // International Journal of Modern Physics B. 2020. Vol.34, Iss.7, Article ID 2050052.
62. Erkaboev U.I., R.G.Rakhimov. Modeling of Shubnikov-de Haas oscillations in narrow band gap semiconductors under the effect of temperature and microwave field // Scientific Bulletin of Namangan State University. 2020. Vol.2, Iss.11. pp.27-35
63. Gulyamov G., Erkaboev U.I., Sayidov N.A., Rakhimov R.G. The influence of temperature on magnetic quantum effects in semiconductor structures // Journal of Applied Science and Engineering. 2020. Vol.23, Iss.3, pp. 453–460.
64. Erkaboev U.I., Gulyamov G., Mirzaev J.I., Rakhimov R.G., Sayidov N.A. Calculation of the Fermi–Dirac Function Distribution in Two-Dimensional Semiconductor Materials at High Temperatures and Weak Magnetic Fields // Nano. 2021. Vol.16, Iss.9. Article ID 2150102.
65. Erkaboev U.I., R.G.Rakhimov. Modeling the influence of temperature on electron landau levels in semiconductors // Scientific Bulletin of Namangan State University. 2020. Vol.2, Iss.12. pp.36-42
66. Erkaboev U.I., Gulyamov G., Mirzaev J.I., Rakhimov R.G., Sayidov N.A. Calculation of the Fermi-Dirac Function Distribution in Two-Dimensional Semiconductor Materials at High Temperatures and Weak Magnetic Fields // Nano. 2021. Vol.16, Iss.9, Article ID 2150102.
67. Erkaboev U.I., Rakhimov R.G., Sayidov N.A., Mirzaev J.I. Modeling the temperature dependence of the density oscillation of energy states in two-dimensional electronic gases under the impact of a longitudinal and transversal quantum magnetic fields // Indian Journal of Physics. 2022. Vol.96, Iss.10, Article ID 02435.
68. Erkaboev U.I., Negmatov U.M., Rakhimov R.G., Mirzaev J.I., Sayidov N.A. Influence of a quantizing magnetic field on the Fermi energy oscillations in two-dimensional semiconductors // International Journal of Applied Science and Engineering. 2022. Vol.19, Iss.2, Article ID 2021123.
69. Erkaboev U.I., Gulyamov G., Rakhimov R.G. A new method for determining the bandgap in semiconductors in presence of external action taking into account lattice vibrations // Indian Journal of Physics. 2022. Vol.96, Iss.8, pp. 2359-2368.
70. U. Erkaboev, R. Rakhimov, J. Mirzaev, U. Negmatov, N. Sayidov. Influence of the two-dimensional density of states on the temperature dependence of the electrical conductivity oscillations in heterostructures with quantum wells // International Journal of Modern Physics B. **38**(15), Article ID 2450185 (2024).
71. U.I. Erkaboev, R.G. Rakhimov. Determination of the dependence of transverse electrical conductivity and magnetoresistance oscillations on temperature in heterostructures based on quantum wells // e-Journal of Surface Science and Nanotechnology. **22**(2), pp.98-106. (2024)

72. U.I. Erkaboev, N.A. Sayidov, J.I. Mirzaev, R.G. Rakhimov. Determination of the temperature dependence of the Fermi energy oscillations in nanostructured semiconductor materials in the presence of a quantizing magnetic field // Euroasian Journal of Semiconductors Science and Engineering. **3**(2), pp.47-52 (2021).
73. U.I. Erkaboev, N.A. Sayidov, U.M.Negmatov, J.I. Mirzaev, R.G. Rakhimov. Influence temperature and strong magnetic field on oscillations of density of energy states in heterostructures with quantum wells HgCdTe/CdHgTe // E3S Web of Conferences. **401**, 01090 (2023)
74. U.I. Erkaboev, N.A. Sayidov, U.M.Negmatov, R.G. Rakhimov, J.I. Mirzaev. Temperature dependence of width band gap in $\text{In}_x\text{Ga}_{1-x}\text{As}$ quantum well in presence of transverse strong magnetic field // E3S Web of Conferences. **401**, 04042 (2023)
75. Erkaboev U.I., Rakhimov R.G., Sayidov N.A., Mirzaev J.I. Modeling the temperature dependence of the density oscillation of energy states in two-dimensional electronic gases under the impact of a longitudinal and transversal quantum magnetic fields // Indian Journal of Physics. 2023. Vol.97, Iss.4, 99.1061-1070.
76. G. Gulyamov, U.I. Erkaboev, R.G. Rakhimov, J.I. Mirzaev, N.A. Sayidov. Determination of the dependence of the two-dimensional combined density of states on external factors in quantum-dimensional heterostructures // Modern Physics Letters B. 2023. Vol. 37, Iss.10, Article ID 2350015.
77. U.I. Erkaboev, R.G. Rakhimov. Determination of the dependence of the oscillation of transverse electrical conductivity and magnetoresistance on temperature in heterostructures based on quantum wells // East European Journal of Physics. 2023. Iss.3, pp.133-145.
78. U.I. Erkaboev, R.G. Rakhimov, J.I. Mirzaev, U.M. Negmatov, N.A. Sayidov. Influence of a magnetic field and temperature on the oscillations of the combined density of states in two-dimensional semiconductor materials // Indian Journal of Physics. 2024. Vol. 98, Iss. 1, pp.189-197.
79. U. Erkaboev, R. Rakhimov, J. Mirzaev, N. Sayidov, U. Negmatov, A. Mashrapov. Determination of the band gap of heterostructural materials with quantum wells at strong magnetic field and high temperature // AIP Conference Proceedings. 2023. Vol. 2789, Iss.1, Article ID 040056.
80. U.I. Erkaboev, R.G. Rakhimov. Simulation of temperature dependence of oscillations of longitudinal magnetoresistance in nanoelectronic semiconductor materials // e-Prime-Advances in Electrical Engineering, Electronics and Energy. 2023. Vol. 5, Article ID 100236.
81. U.I. Erkaboev, R.G. Rakhimov, N.Y. Azimova. Determination of oscillations of the density of energy states in nanoscale semiconductor materials at different temperatures and quantizing magnetic fields // Global Scientific Review. 2023. Vol.12, pp.33-49
82. U.I. Erkaboev, R.G. Rakhimov, U.M. Negmatov, N.A. Sayidov, J.I. Mirzaev. Influence of a strong magnetic field on the temperature dependence of the two-dimensional combined density of states in InGaN/GaN quantum well heterostructures // Romanian Journal of Physics. 2023. Vol. 68, Iss. 5-6, pp.614-1.

83. R. Rakhimov, U. Erkaboev. Modeling of Shubnikov-de Haas oscillations in narrow band gap semiconductors under the effect of temperature and microwave field // Scientific Bulletin of Namangan State University. 2020. Vol.2, Iss. 11, pp.27-35.
84. U. Erkaboev, R. Rakhimov, J. Mirzaev, N. Sayidov, U. Negmatov, M. Abduxalimov. Calculation of oscillations in the density of energy states in heterostructural materials with quantum wells // AIP Conference Proceedings. Vol. 2789, Iss.1, Article ID 040055.
85. R. Rakhimov, U. Erkaboev. Modeling the influence of temperature on electron Landau levels in semiconductors // Scientific and Technical Journal of Namangan Institute of Engineering and Technology. 2020. Vol. 2, Iss. 12, pp.36-42.
86. U.I. Erkaboev, R.G. Rakhimov. Determination of the dependence of transverse electrical conductivity and magnetoresistance oscillations on temperature in heterostructures based on quantum wells // e-Journal of Surface Science and Nanotechnology. 2023
87. У.И. Эркабоев, Р.Г. Рахимов, Ж.И. Мирзаев, Н.А. Сайидов, У.М. Негматов. Вычисление осцилляции плотности энергетических состояний в гетеронаноструктурных материалах при наличии продольного и поперечного сильного магнитного поля // Научные основы использования информационных технологий нового уровня и современные проблемы автоматизации : I Международной научной конференции, 25-26 апреля 2022 года. стр.341-344.
88. U.I. Erkaboev, R.G. Rakhimov. Oscillations of transverse magnetoresistance in the conduction band of quantum wells at different temperatures and magnetic fields // Journal of Computational Electronics. 2024. Vol. 23, Iss. 2, pp.279-290
89. У.И. Эркабоев, Р.Г. Рахимов, Ж.И. Мирзаев, Н.А. Сайидов, У.М. Негматов. Расчеты температурной зависимости энергетического спектра электронов и дырок в разрешенной зоне квантовой ямы при воздействии поперечного квантующего магнитного поля // Научные основы использования информационных технологий нового уровня и современные проблемы автоматизации : I Международной научной конференции, 25-26 апреля 2022 года. стр.344-347.
90. U.I. Erkaboev, R.G. Rakhimov, J.I. Mirzaev, N.A. Sayidov, U.M. Negmatov. Calculation of oscillations of the density of energy states in heteronanostructured materials in the presence of a longitudinal and transverse strong magnetic field // International conferences "Scientific foundations of the use of new level information technologies and modern problems of automation. 2022. pp.341-344
91. U.I. Erkaboev, R.G. Rakhimov, J.I. Mirzaev, N.A. Sayidov, U.M. Negmatov. Calculations of the temperature dependence of the energy spectrum of electrons and holes in the allowed zone of a quantum well under the influence of a transverse quantizing magnetic field // International conferences "Scientific foundations of the use of new level information technologies and modern problems of automation. 2022. pp.344-347
92. R.G. Rakhimov, U.I. Erkaboev. Modeling of Shubnikov-de Haas oscillations in narrow-band semiconductors under the influence of temperature and microwave fields // Scientific Bulletin of Namangan State University. 2022. Vol. 4, Iss.4, pp.242-246.
93. R.G. Rakhimov. The advantages of innovative and pedagogical approaches in the education system // Scientific-technical journal of NamIET. Vol. 5, Iss. 3, pp.292-296 (2020)

94. Р.Г. Рахимов, У.И. Эркабоев. Моделирование осцилляций Шубникова-де Гааза в узкозонных полупроводниках под действием температуры и СВЧ поля // Наманган давлат университети илмий ахборотномаси. 2019. Vol. 4, Iss. 4, pp.242-246
95. U.I. Erkaboev, R.G. Rakhimov, J.I. Mirzaev, N.A. Sayidov, U.M. Negmatov. Modeling the Temperature Dependence of Shubnikov-De Haas Oscillations in Light-Induced Nanostructured Semiconductors // East European Journal of Physics. 2024. Iss. 1, pp. 485-492.
96. M. Dadamirzaev, U. Erkaboev, N. Sharibaev, R. Rakhimov. Simulation the effects of temperature and magnetic field on the density of surface states in semiconductor heterostructures // Iranian Journal of Physics Research. 2024
97. U.I. Erkaboev, N.Yu. Sharibaev, M.G. Dadamirzaev, R.G. Rakhimov. Effect of temperature and magnetic field on the density of surface states in semiconductor heterostructures // e-Prime-Advances in Electrical Engineering, Electronics and Energy. 2024. Vol.10, Article ID 100815.
98. U.I. Erkaboev, Sh.A. Ruzaliev, R.G. Rakhimov, N.A. Sayidov. Modeling Temperature Dependence of The Combined Density of States in Heterostructures with Quantum Wells Under the Influence of a Quantizing Magnetic Field // East European Journal of Physics. 2024. Iss.3, pp.270-277.
99. U.I. Erkaboev, N.Yu. Sharibaev, M.G. Dadamirzaev, R.G. Rakhimov. Modeling influence of temperature and magnetic field on the density of surface states in semiconductor structures // Indian Journal of Physics. 2024.
100. U.I. Erkaboev, G. Gulyamov, M. Dadamirzaev, R.G. Rakhimov, J.I. Mirzaev, N.A. Sayidov, U.M. Negmatov. The influence of light on transverse magnetoresistance oscillations in low-dimensional semiconductor structures // Indian Journal of Physics. 2024.
101. Р.Г. Рахимов. Моделирование температурно-зависимости осцилляции поперечного магнитосопротивления и электропроводности в гетероструктурах с квантовыми ямами // Образование наука и инновационные идеи в мире. 2024. Vol. 37, Iss. 5, pp.137-152.
102. N. Sharibaev, A. Jabborov, R. Rakhimov, Sh. Korabayev, R. Sapayev. A new method for digital processing cardio signals using the wavelet function // BIO Web of Conferences. 2024. Vol. 130, Article ID 04008.
103. A.M. Sultanov, E.K. Yusupov, R.G. Rakhimov. Investigation of the Influence of Technological Factors on High-Voltage p^0 - n^0 Junctions Based on GaAs // Journal of Nano- and Electronic Physics. 2024. Vol. 16, Iss. 2, Article ID 01006.
104. U.I. Erkaboev, R.G. Rakhimov, J.I. Mirzaev, N.A. Sayidov, U.M. Negmatov. Influence of temperature and light on magnetoresistance and electrical conductivity oscillations in quantum well heterostructured semiconductors // Romanian Journal of Physics. 2024. Vol. 69, pp.610
105. У.И. Эркабоев, Р.Г. Рахимов, Ж.И. Мирзаев, Н.А. Сайидов, У.М. Негматов, С.И. Гайратов. Влияние температуры на осцилляции поперечного магнитосопротивления в низкоразмерных полупроводниковых структурах // Namangan davlat universiteti Ilmiy axborotnomasi. 2023. Iss. 8, pp.40-48.

106. U. Erkaboev, N. Sayidov, R. Raximov, U. Negmatov, J. Mirzaev. Kvant o 'rali geterostrukturalarda kombinatsiyalangan holatlar zichligiga magnit maydon va haroratning ta'siri // Namangan davlat universiteti Ilmiy axborotnomasi. 2023. Iss. 6, pp.16-22
107. У.И. Эркабоев, Р.Г. Рахимов. Вычисление температурной зависимости поперечной электропроводности в квантовых ямах при воздействии квантующего магнитного поля // II- Международной конференции «Фундаментальные и прикладные проблемы физики полупроводников, микро- и нанoeлектроники». Ташкент, 27-28 октября 2023 г. стр.66-68.
108. R.G.Rakhimov. Simulation of the temperature dependence of the oscillation of magnetosistivity in nanosized semiconductor structures under the exposure to external fields // Web of Technology: Multidimensional Research Journal. 2024. Vol.2, Iss.11, pp.209-221